

Causal Conceptions of Fairness and their Consequences



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(* equal contribution)

[ACIC 2022 / ICML 2022]

Summary

- Unified taxonomy to understand *causal fairness* research field

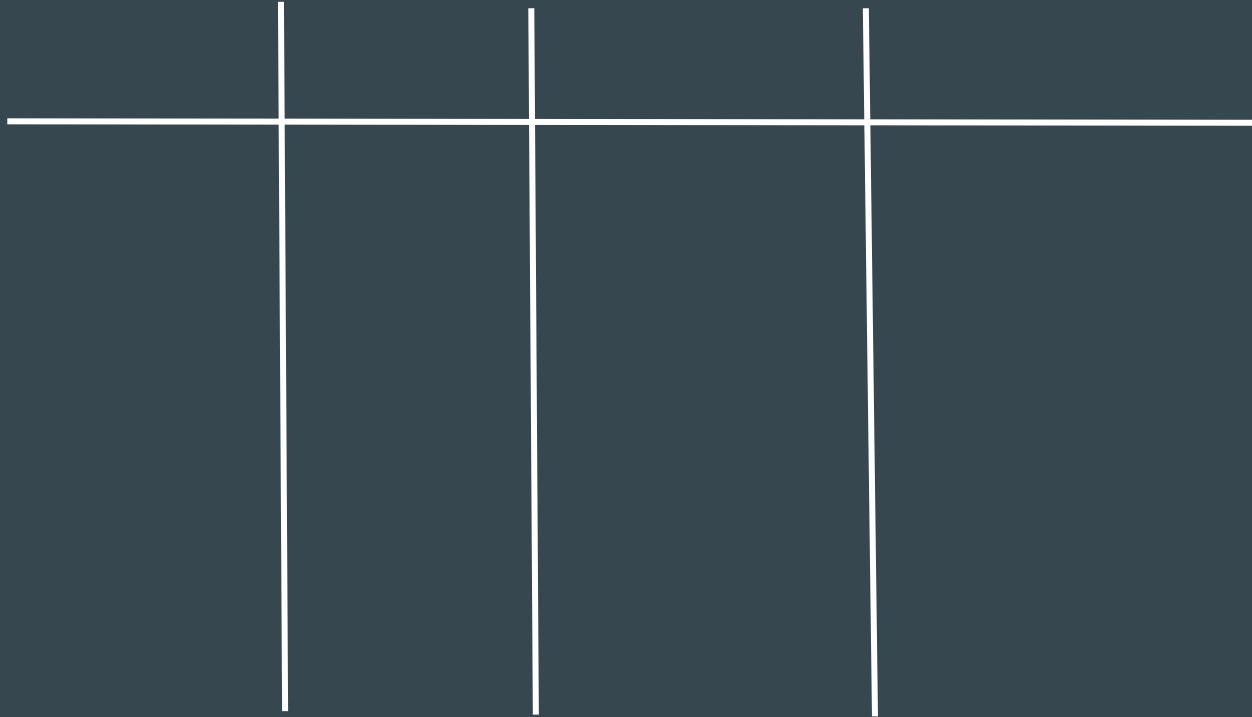
Summary

- Unified taxonomy to understand *causal fairness* research field
- Prominent causal conceptions of algorithmic fairness, if implemented, can harm the groups they were designed to protect


Stylized Example: College Admissions





Stylized Example: College Admissions









Stylized Example: College Admissions

|  Test Score | | | |
|----------------------------------------------------------------------------------------------|--|--|--|
| 73 | | | |
| 65 | | | |
| 80 | | | |
| ... | | | |











Stylized Example: College Admissions

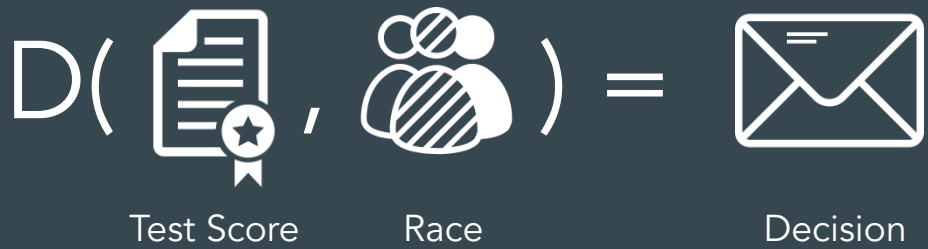
|  Test Score |  Race Group | | |
|----------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------|--|--|
| 73 | Minority | | |
| 65 | Majority | | |
| 80 | Minority | | |
| ... | ... | | |

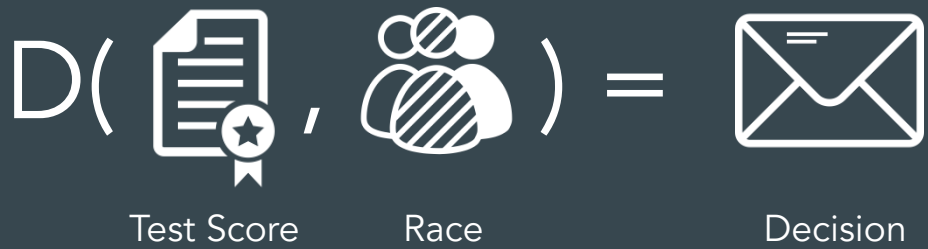
Stylized Example: College Admissions

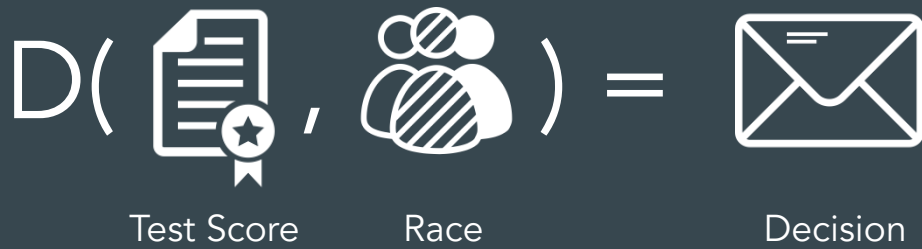
|  Test Score |  Race Group |  Decision | |
|----------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------|--|
| 73 | Minority |  | |
| 65 | Majority |  | |
| 80 | Minority |  | |
| ... | ... | ... | |

Stylized Example: College Admissions

|  Test Score |  Race Group |  Decision |  Degree Attainment |
|----------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------|
| 73 | Minority |  |  |
| 65 | Majority |  |  |
| 80 | Minority |  |  |
| ... | ... | ... | ... |








Degree
Attainment



Class Diversity





How to ensure that D is fair?



[Part 1: *causal fairness*
overview + taxonomy]

Traditional fairness definitions

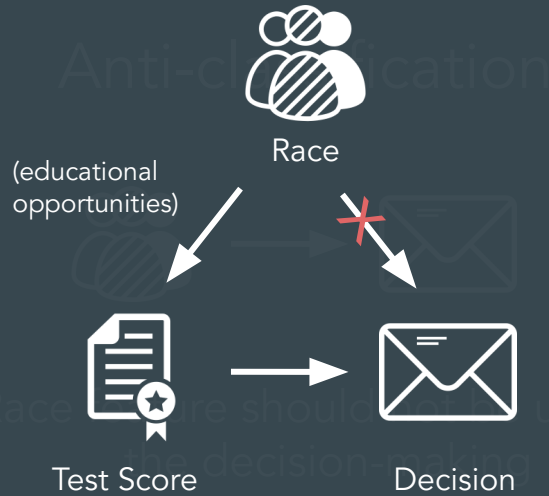
Anti-classification



Race feature should not be used in
the decision-making

$$D(\text{Race}=95, \text{Minority}) =$$
$$D(\text{Race}=95, \text{Majority})$$

Causal Fairness Motivation



Race may still *indirectly* affect decisions

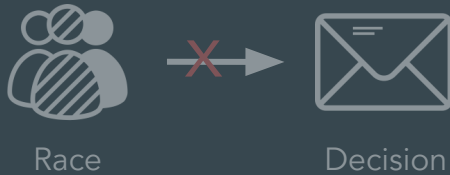
Causal Fairness Taxonomy



Family 1: Limit direct and indirect effects of race on decision

Traditional fairness definitions

Anti-classification



Race feature should not be used in the decision-making

$$D(\text{📄}=95, \text{👤}=Minority) = \\ D(\text{📄}=95, \text{👤}=Majority)$$

Classification parity

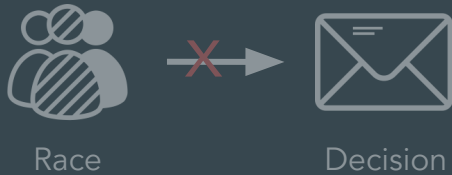


Model performance should be the same across groups

Precision = % of admits who successfully obtain a bachelor's degree

Traditional fairness definitions

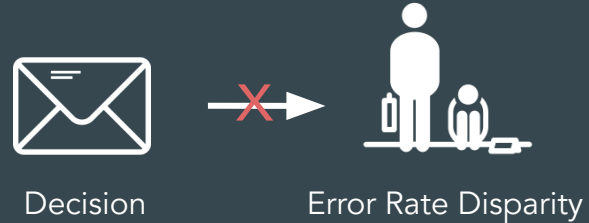
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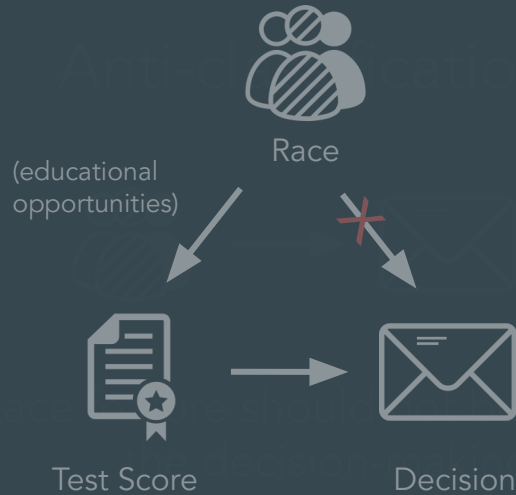
Classification parity



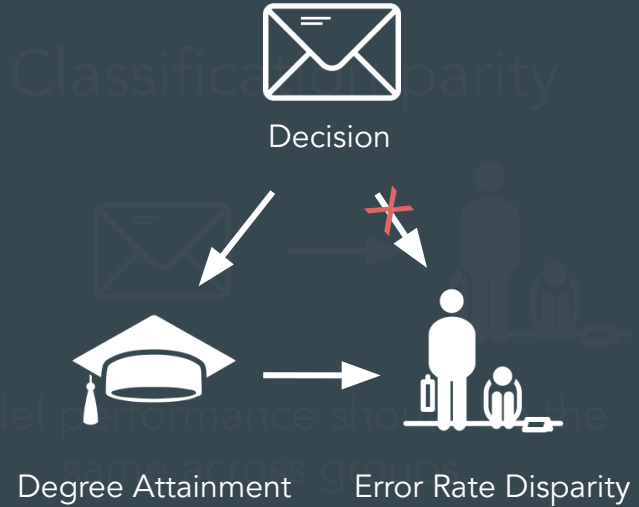
Model performance should be the same across groups

$$\text{Minority group precision} = \text{Majority group precision}$$

Causal Fairness Motivation

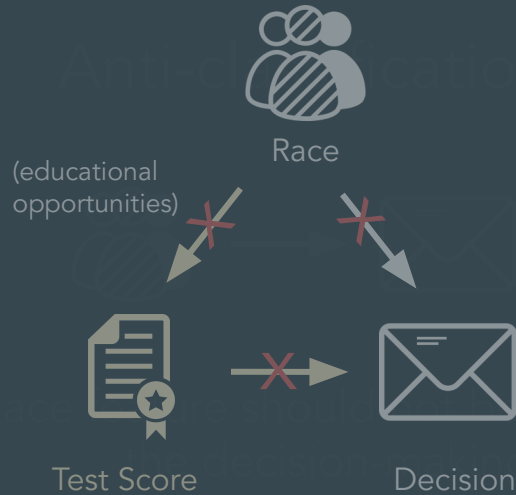


Race may still *indirectly* affect decisions

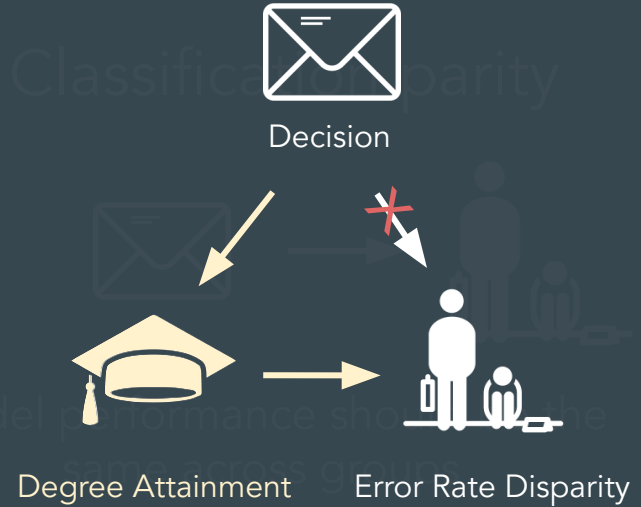


Decisions may affect graduation, altering error rates

Causal Fairness Taxonomy



Family 1: Limit direct and indirect effects of race on decision



Family 2: Model performance should be counterfactually equal between groups

Causal fairness taxonomy [see paper]

Family 1: Limit direct and indirect effects of race on decision

- Counterfactual fairness
- Path-specific fairness

Family 2: Limit counterfactual disparities between groups

- Counterfactual equalized odds
- Counterfactual predictive parity
- Principal fairness

Causal fairness taxonomy [see paper]

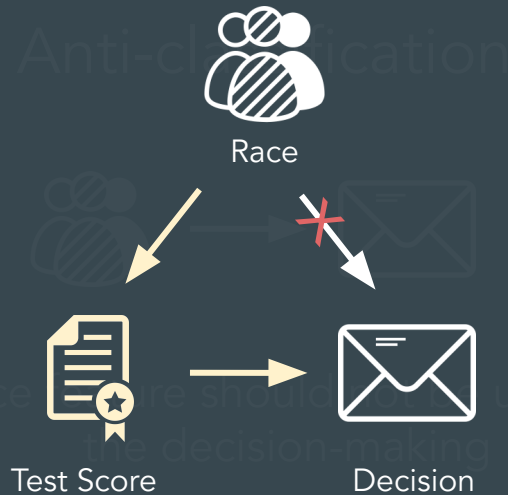
Family 1: Limit direct and indirect effects of race on decision

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Counterfactual Fairness



Family 1: Limit direct and indirect effects of race on decision

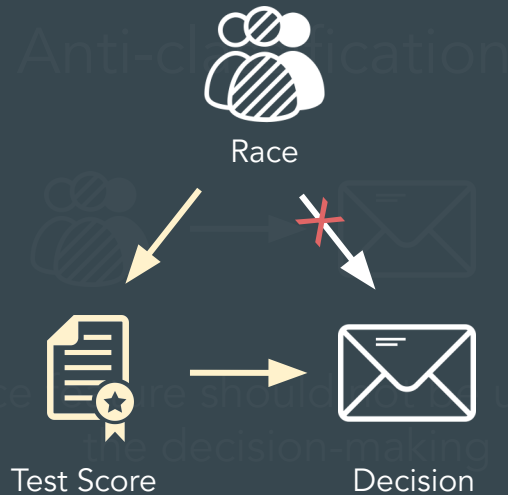
Classification parity

Given a subset of applicants with the exact same feature values, admissions rate should not change *in a counterfactual world in which they belonged to a different race group*

Model performance should be the same across groups

False positive rate (admits who did not graduate) should be equal between groups

Counterfactual Fairness



Family 1: Limit direct and indirect effects of race on decision

Classification parity

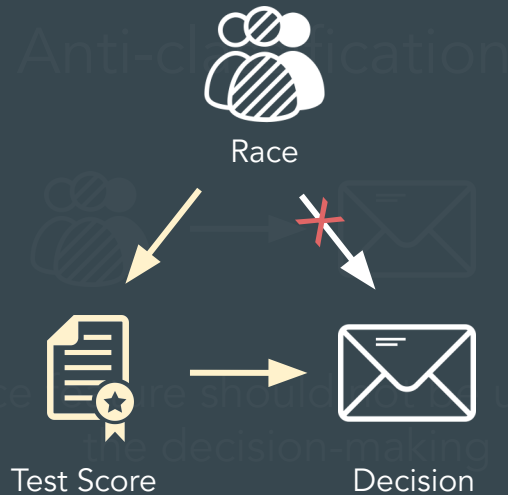
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Model performance should be the same across groups

[Important caveat: counterfactuals of race are epistemologically problematic]

(not graduate) should be equal between groups

Counterfactual Fairness

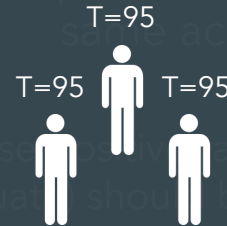


Family 1: Limit direct and indirect effects of race on decision

Classification parity

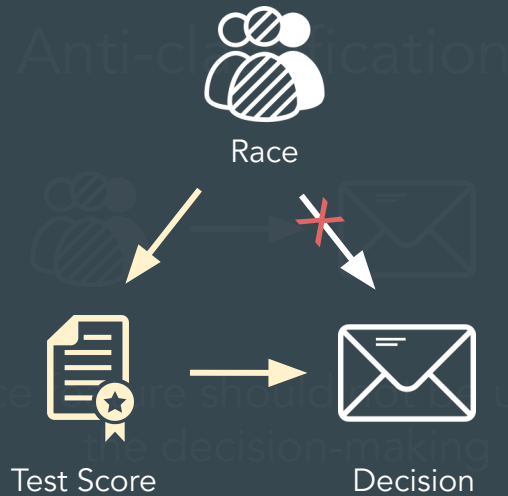
Given a subset of applicants with the exact same feature values, admissions rate should not change *in a counterfactual world in which they belonged to a different race group*

Model performance should be the same across groups



Majority
(real world)

Counterfactual Fairness



Family 1: Limit direct and indirect effects of race on decision

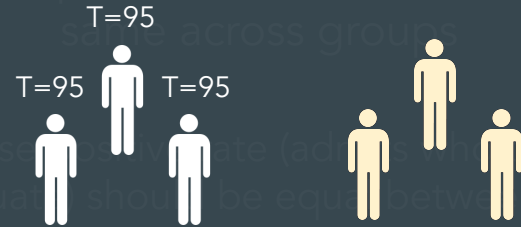
Classification parity

Given a subset of applicants with the exact same feature values, admissions rate should not change *in a counterfactual world in which they belonged to a different race group*

Model performance should be the same across groups

Fake test scores should not be used in decision making

Fake graduation rates should not be equal between groups



Majority (real world) Minority (counterfactual world)

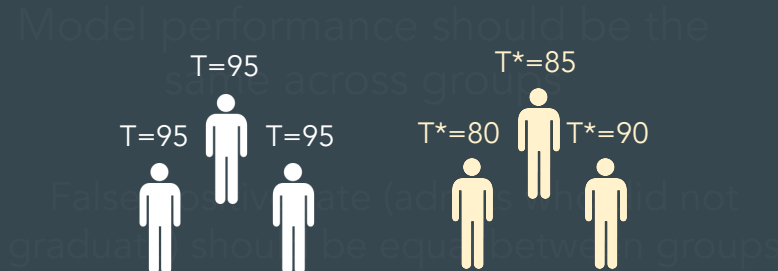
Counterfactual Fairness



Family 1: Limit direct and indirect effects of race on decision

Classification parity

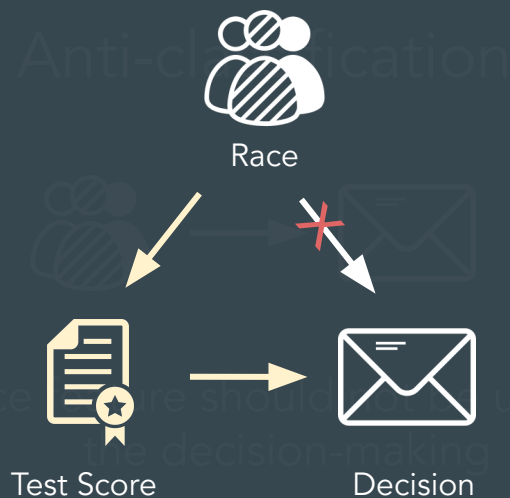
Given a subset of applicants with the exact same feature values, admissions rate should not change *in a counterfactual world in which they belonged to a different race group*



Majority (real world) Minority (counterfactual world)

[T* decreases due to reduced access to educational opportunities]

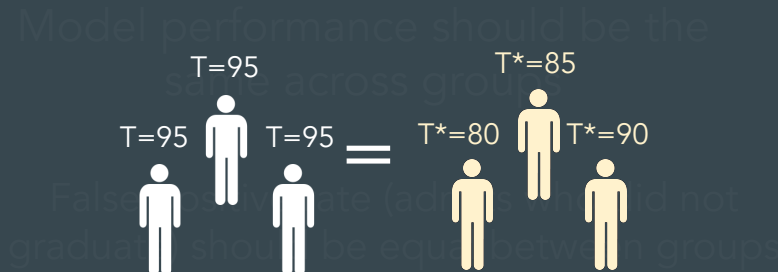
Counterfactual Fairness



Family 1: Limit direct and indirect effects of race on decision

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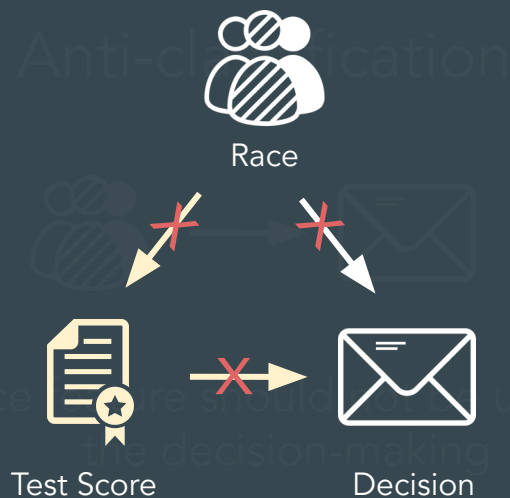
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Majority (real world) Minority (counterfactual world)

[T* decreases due to reduced access to educational opportunities]

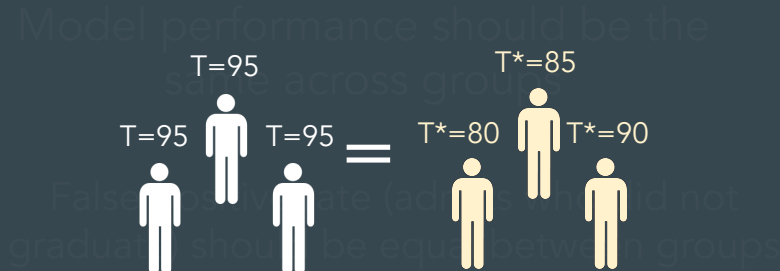
Counterfactual Fairness



Family 1: Limit direct and indirect effects of race on decision

Classification parity

Given a subset of applicants with the exact same feature values, admissions rate should not change *in a counterfactual world in which they belonged to a different race group*



[T* decreases due to reduced access to educational opportunities]

Part 2: What are the downstream consequences of causal fairness?



Counterfactual Fairness

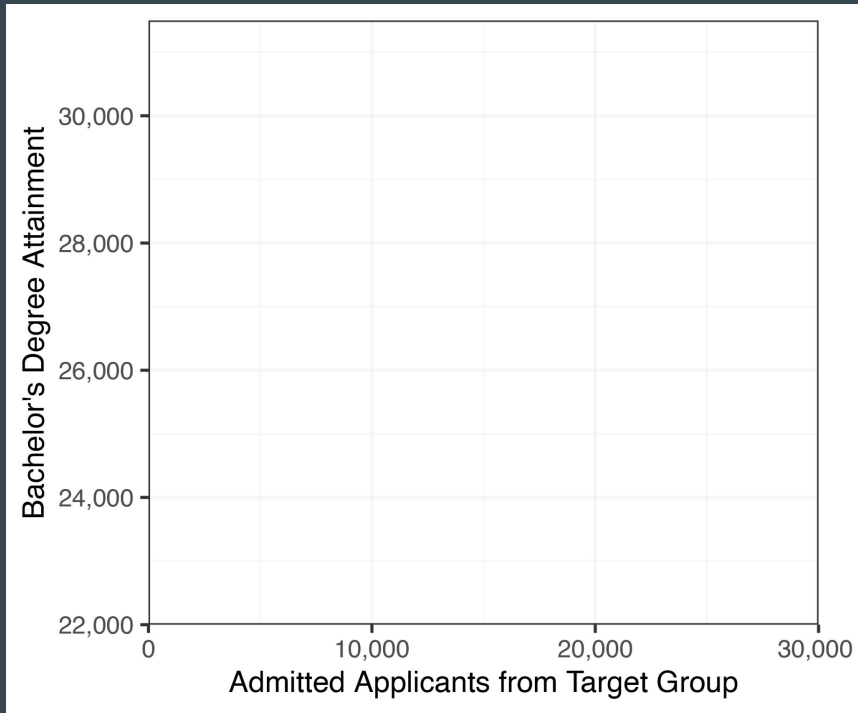


Diversity

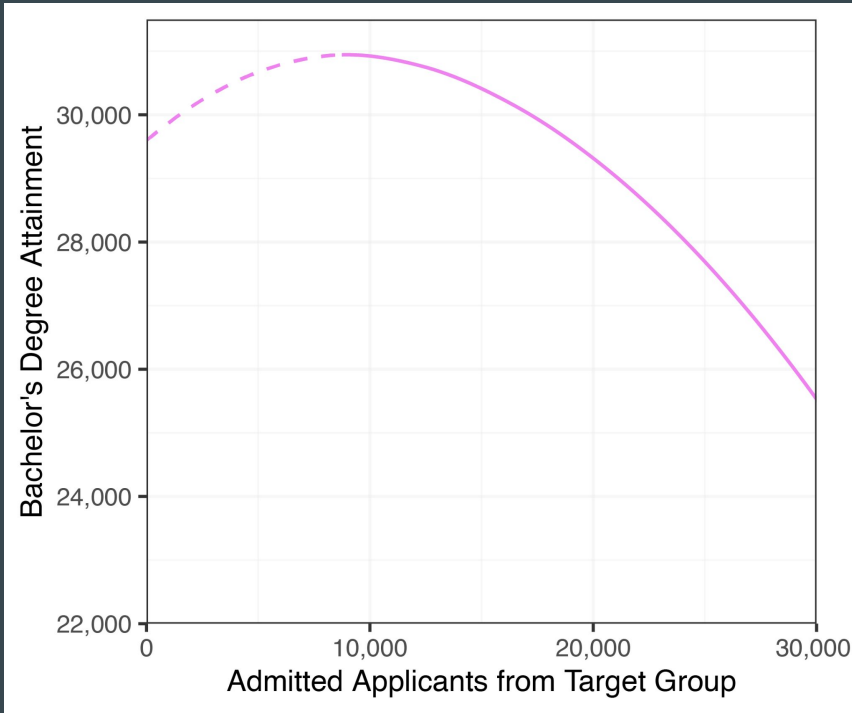


Degree Attainment

Illustrative example

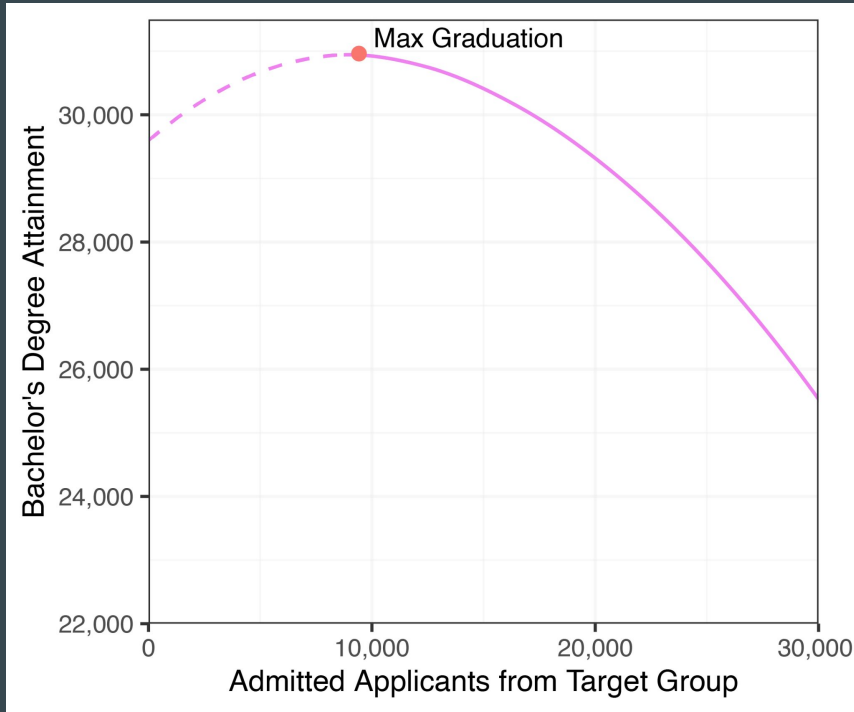


Illustrative example



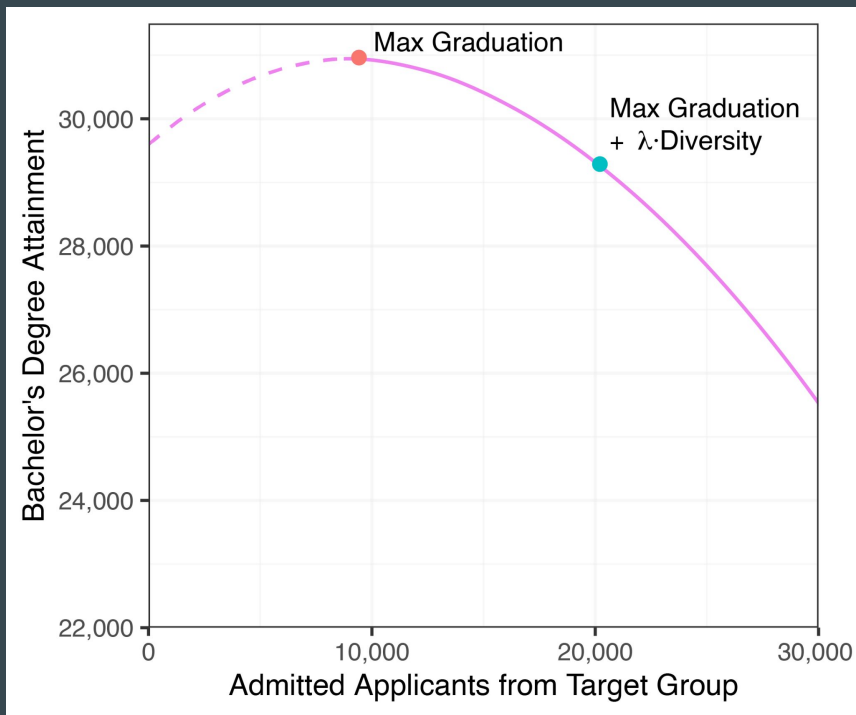
Pareto frontier: different people trade off degree attainment and diversity differently

Illustrative example



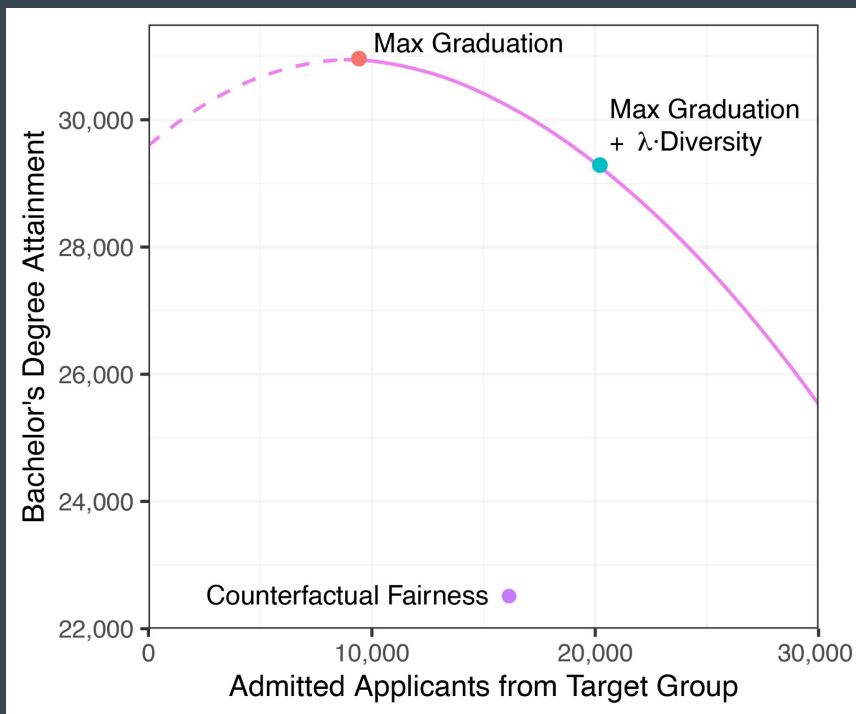
Pareto frontier: different people trade off degree attainment and diversity differently

Illustrative example

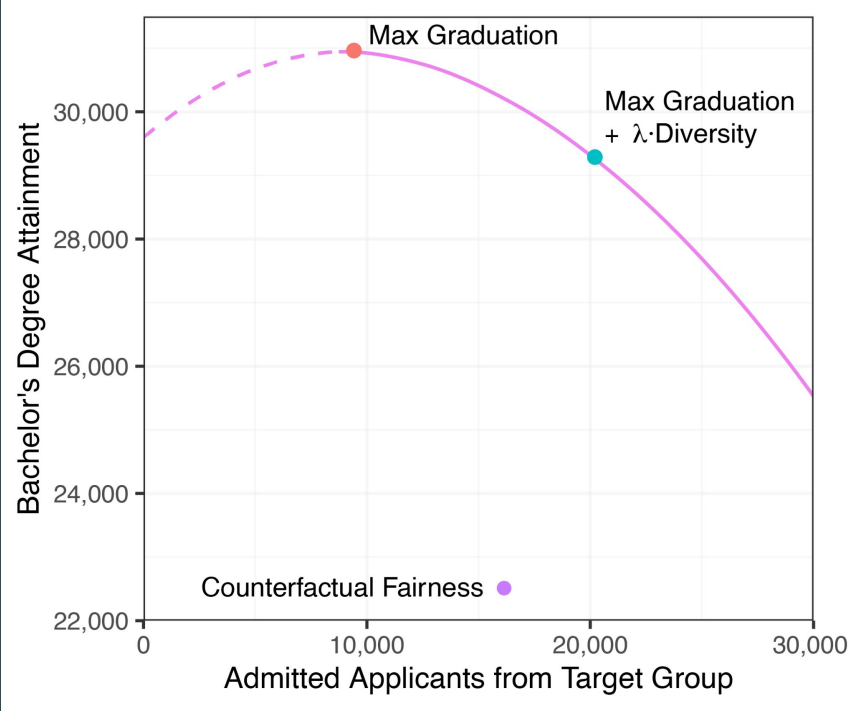


Pareto frontier: different people trade off degree attainment and diversity differently

Illustrative example



Illustrative example

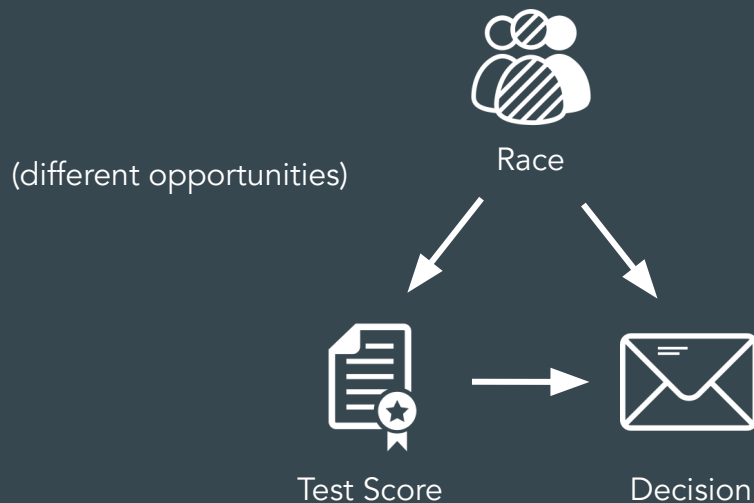


Counterfactual
Fairness

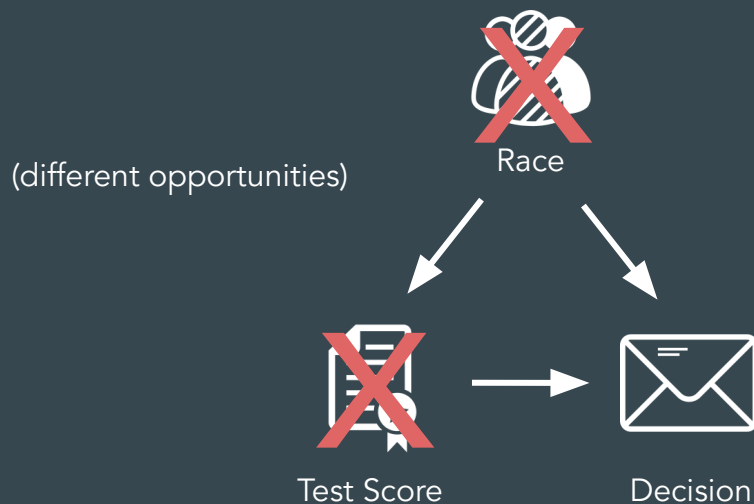


Randomized
Lottery

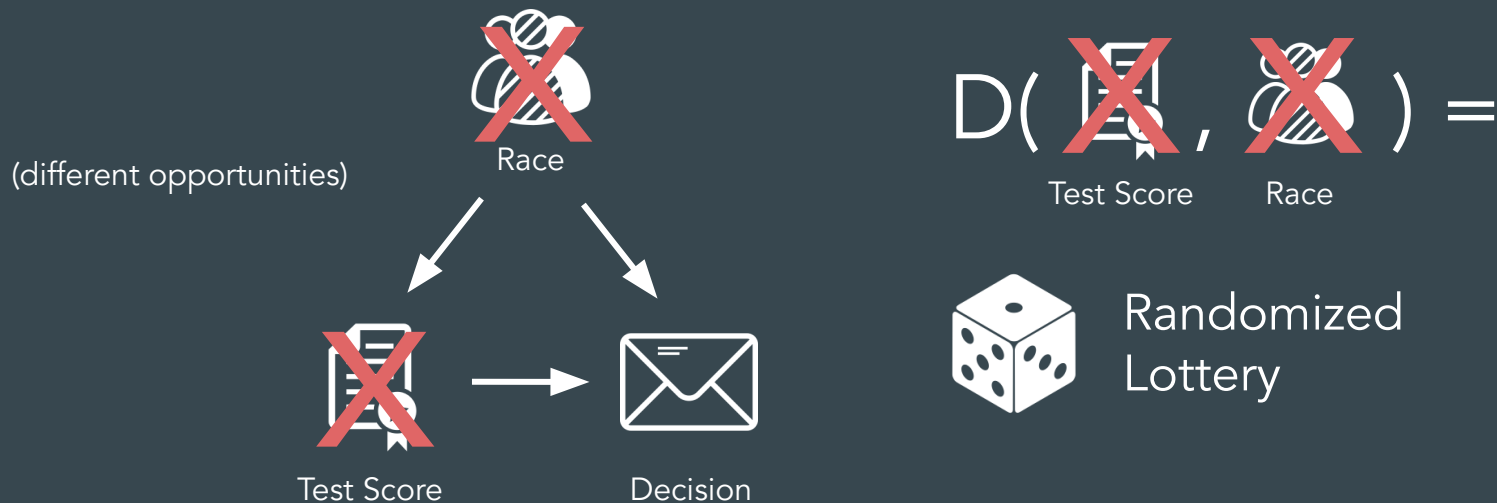
Theoretical result: Under mild assumptions, counterfactual fairness requires decisions to ignore race and all downstream covariates



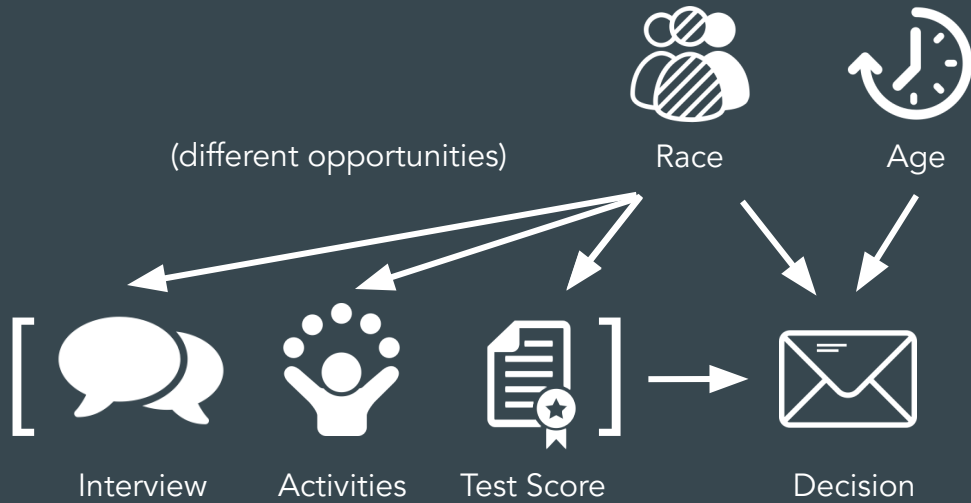
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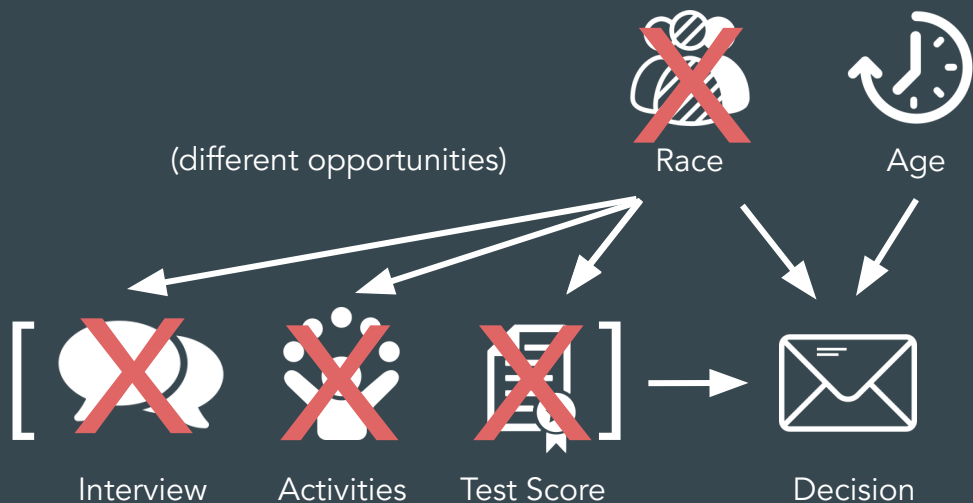
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Decisions based exclusively on age

Proof sketch



$D(T = \text{Low}, \text{Race} = \text{Majority})$



$D(T = \text{Med.}, \text{Race} = \text{Majority})$



$D(T = \text{High.}, \text{Race} = \text{Majority})$



$D(T = \text{Low}, \text{Race} = \text{Majority})$

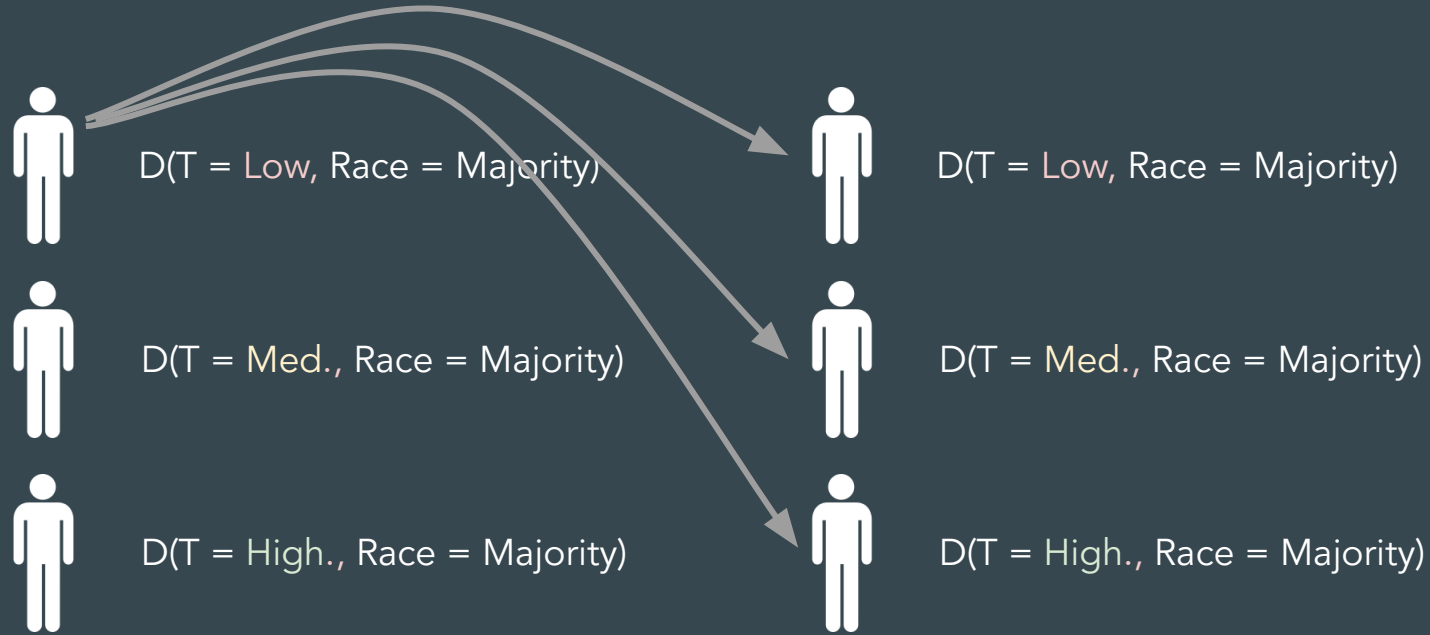


$D(T = \text{Med.}, \text{Race} = \text{Majority})$

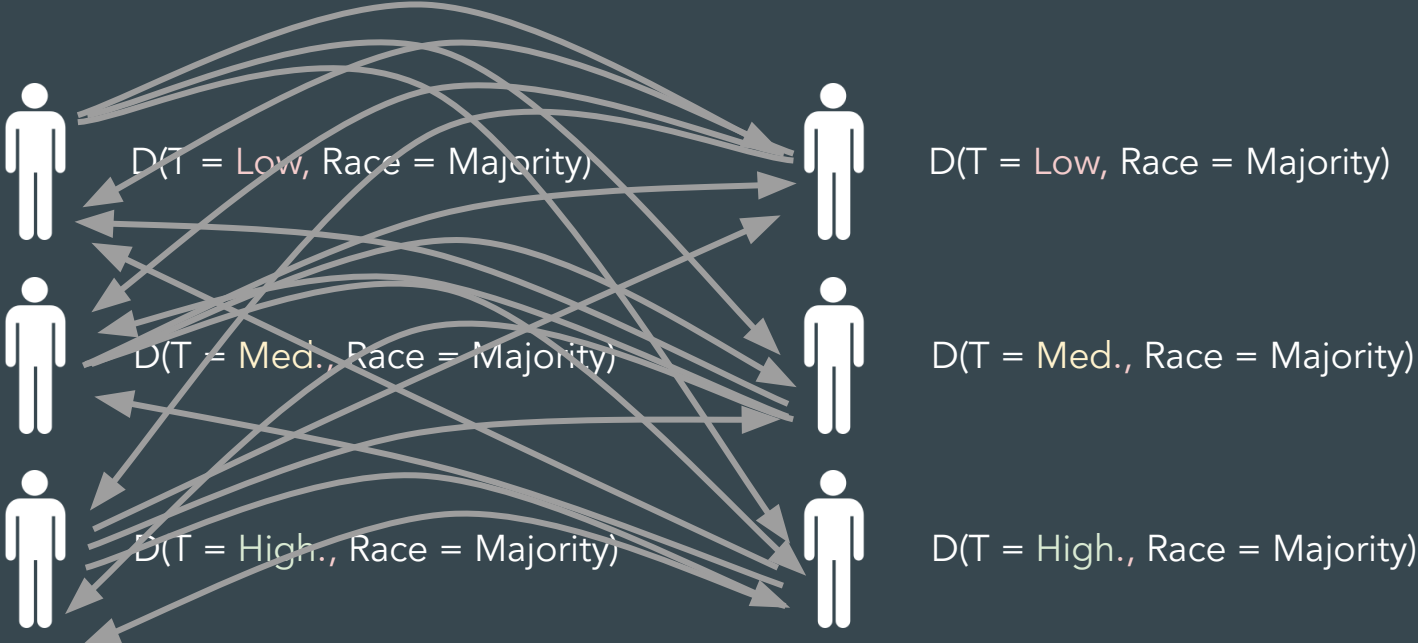


$D(T = \text{High.}, \text{Race} = \text{Majority})$

Proof sketch



Proof sketch



Causal fairness taxonomy [see paper]

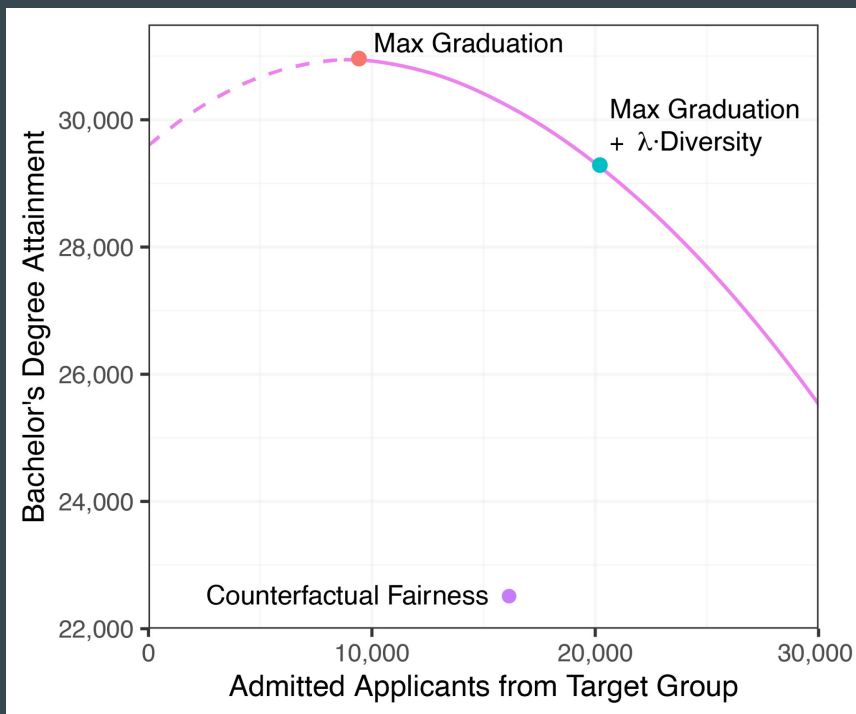
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- Counterfactual fairness
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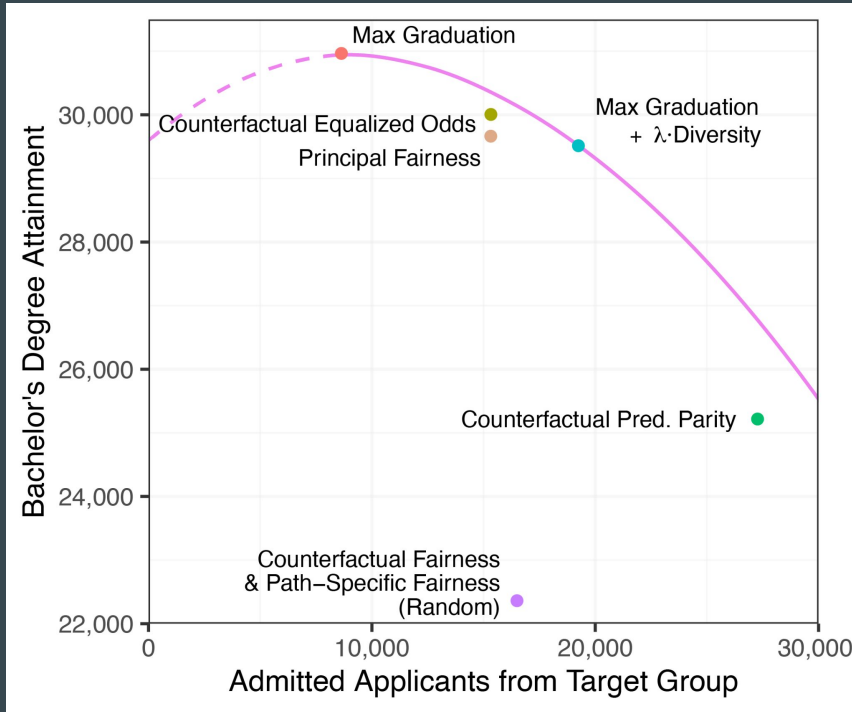
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- Counterfactual equalized odds
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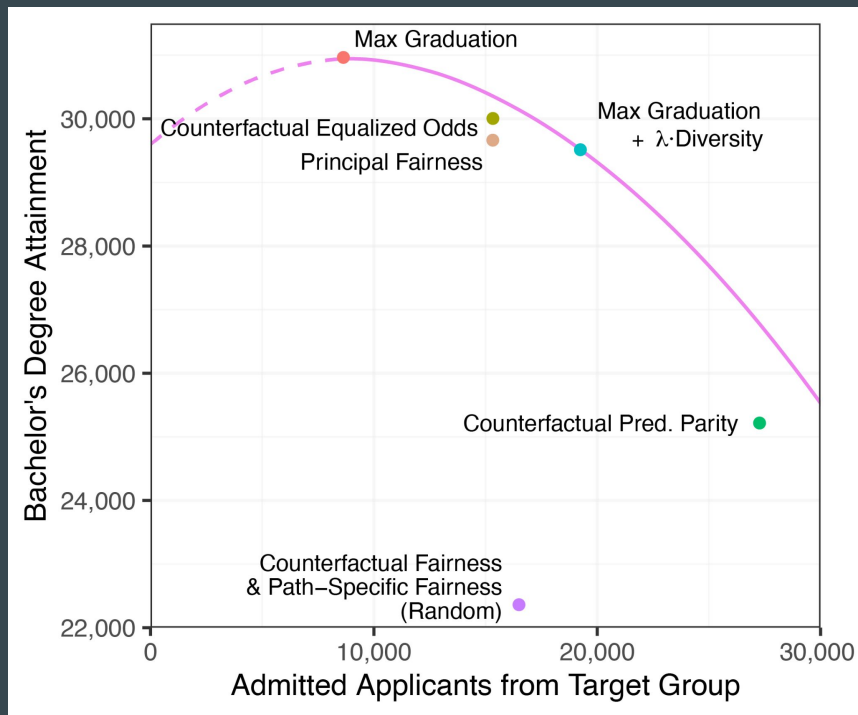
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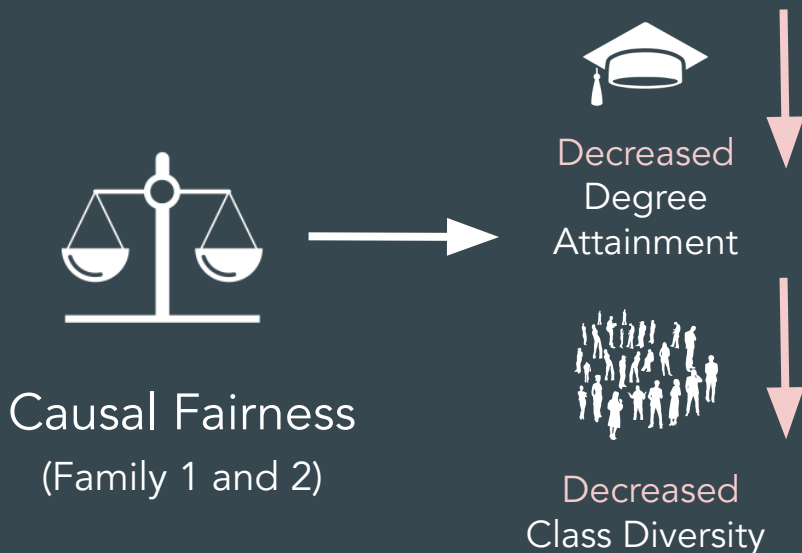
Key theoretical result #2



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In *almost every* case (in a measure theoretic sense)...



Summary

- Causal fairness definitions lead to Pareto inefficient decisions, perversely harming the groups they were designed to protect
- Directly optimizing for desired outcomes (e.g. degree attainment, diversity) may be preferable

Thank You!



[Full Paper](#)

H. Nilforoshan*, J. Gaebler*, R. Shroff, & S. Goel. "Causal Conceptions of Fairness and their Consequences." *International Conference on Machine Learning (ICML 2022)*.

[jgaeb.com

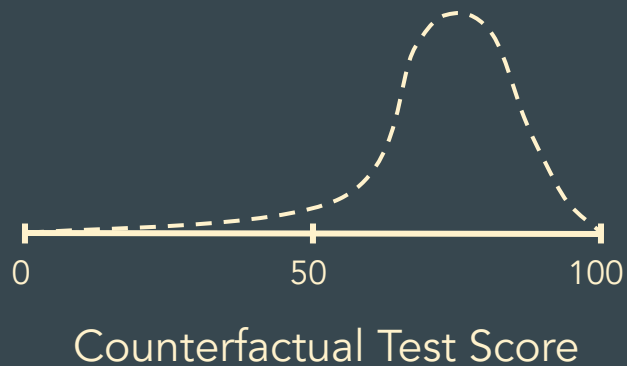
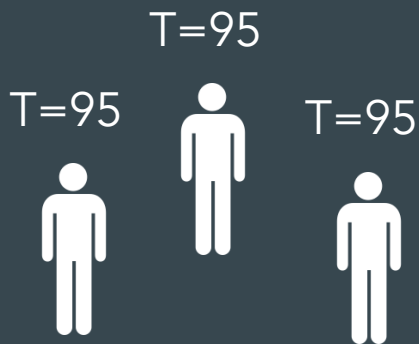
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[hamedn.com

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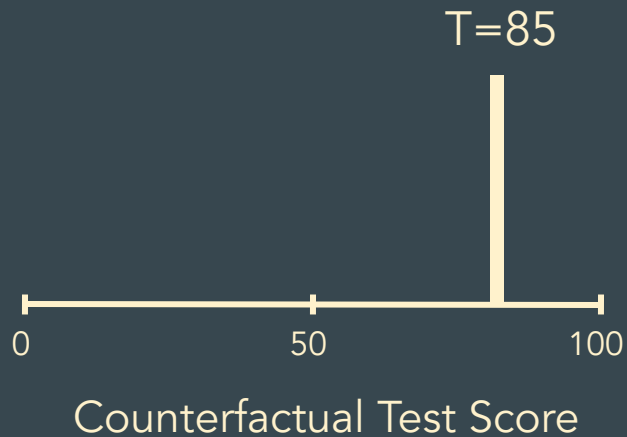
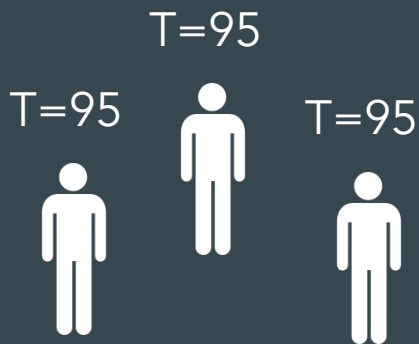
Assumptions

There is variance in the counterfactual distribution of covariates

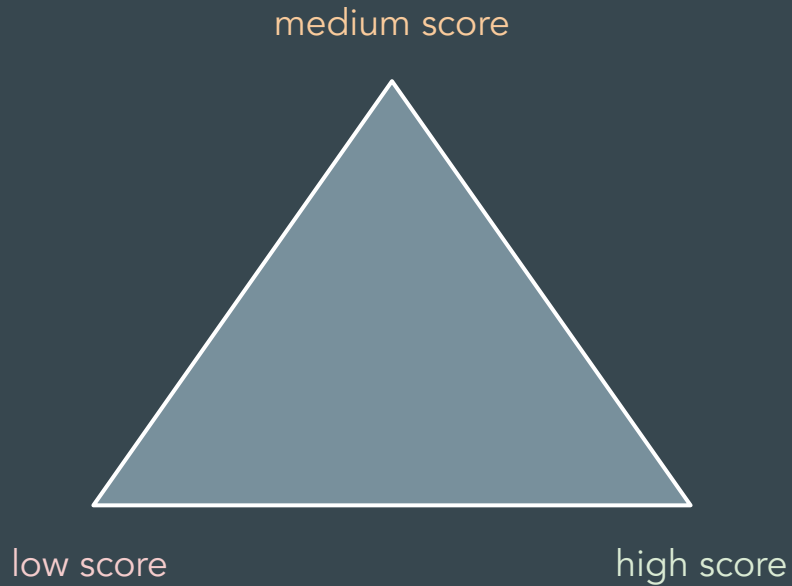


Assumptions

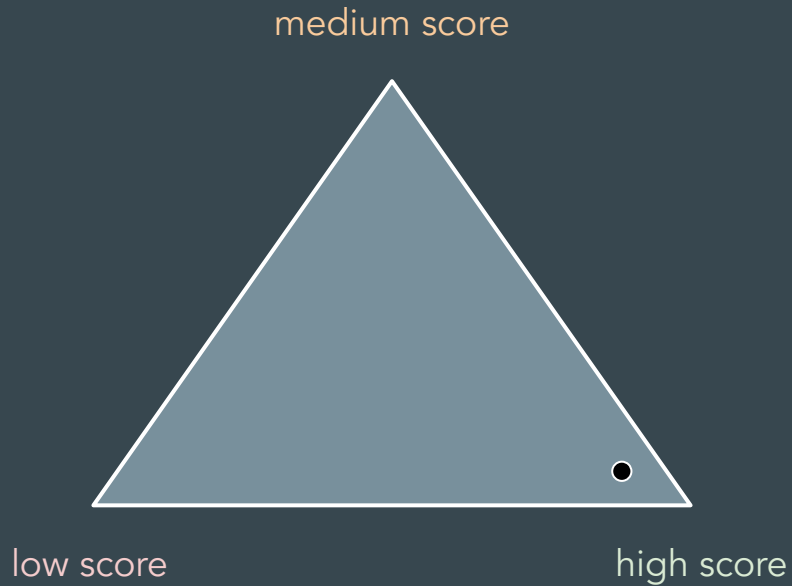
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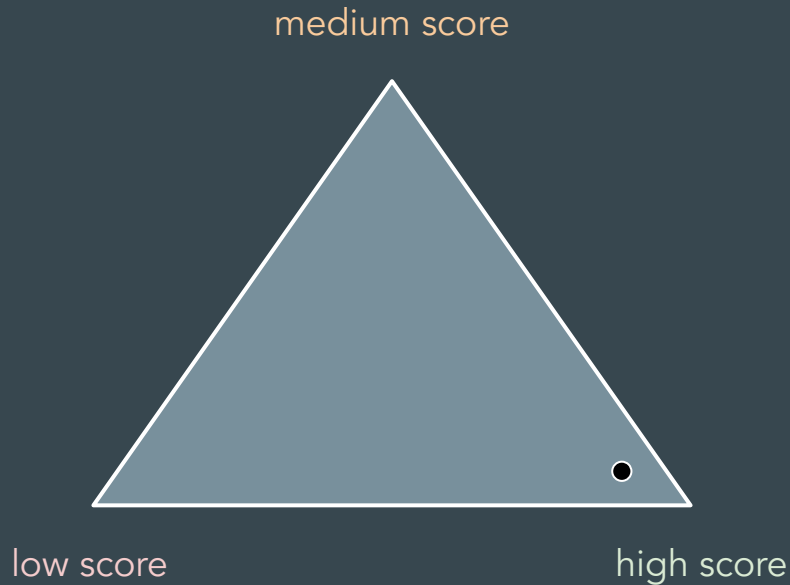
What do we mean by “almost every”?



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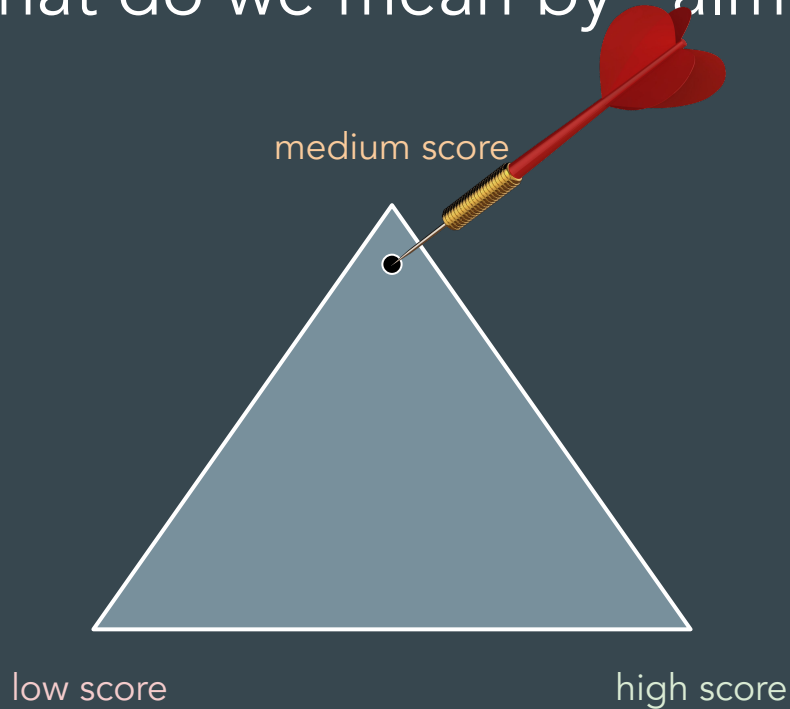


$$P(\text{📄} = \text{low}) = 0.05$$

$$P(\text{📄} = \text{medium}) = 0.05$$

$$P(\text{📄} = \text{high}) = 0.90$$

What do we mean by "almost every"?

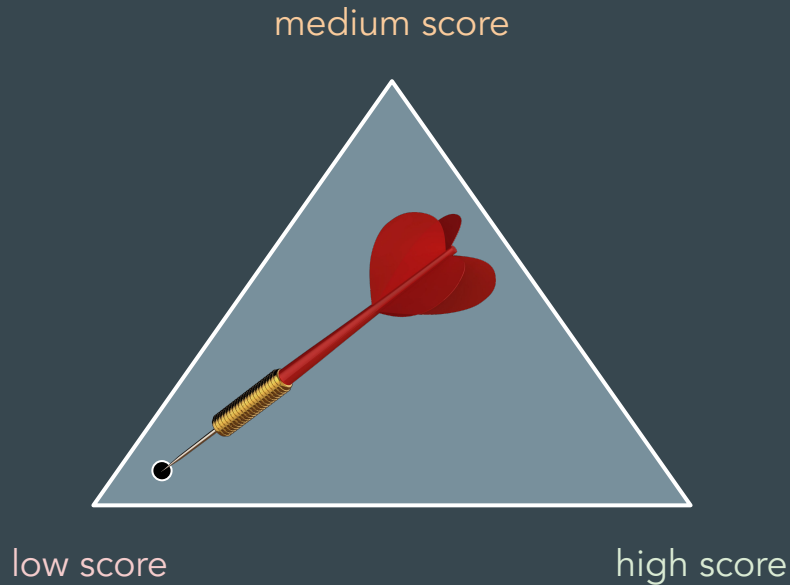


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What do we mean by "almost every"?



$$P(\text{📄} = \text{low}) = 0.90$$

$$P(\text{📄} = \text{medium}) = 0.05$$

$$P(\text{📄} = \text{high}) = 0.05$$

$P(\downarrow \text{👥} \downarrow \text{🎓} \text{ Pareto Inefficient} \mid \text{🎯 Randomly Chosen Distribution}) = 1.0$

Simulation variables

